Joint Spectrum Allocation and Power Control for Multihop Cognitive Radio Networks

Wei Wang, Member, IEEE, Kang G. Shin, Fellow, IEEE, and Wenbo Wang, Member, IEEE

Abstract—We propose a new framework of joint spectrum allocation and power control to utilize open spectrum bands in cognitive radio networks (CRNs) by considering both interference temperature constraints and spectrum dynamics. We first address a simpler problem for the case of a single flow. A TDM-based power-control strategy is adopted to achieve maximum end-to-end throughput by choosing an appropriate multihop route and spectrum combination for each single flow. Then, the simpler solution is extended to the multilayer case in which interflow interference and cumulative interference temperature must be considered. Considering the overhead of switching route and spectrum, the optimal waiting time before making a switch is derived. Our in-depth simulation study has shown that the proposed algorithms utilize spectrum more efficiently than other existing algorithms.

Index Terms—Cognitive radio networks (CRNs), multiple-hop flows, spectrum allocation, power control.

1 INTRODUCTION

The problem of severely unbalanced, and hence inefficient, spectrum utilization [1] has been attracting considerable attention from academia and industry as the target for remedying the anticipated spectrum shortage in accommodating rapidly growing wireless applications and user population. Static spectrum allocation regulations are known to be the main culprit of inefficient spectrum utilization because a licensed spectrum band can be used only by its primary/licensed users. Unlicensed users are not allowed to use the spectrum band even when it is left idle by the primary users.

To mitigate this problem, the FCC is considering the fixed spectrum license regulation to be relaxed, thus allowing unlicensed/secondary users (SUs) to access idle spectrum bands dynamically, i.e., secondary users can utilize the spectrum as long as they do not interfere with the primary users. Cognitive radios [2] and their inter-networking are an important means of realizing this spectrum utilization improvement. The authors of [3], [4] discussed the main characteristics of CRNs, including signal processing, spectrum utilization, and adaptive procedures. Note, however, that most previous research on cognitive radios focused on single-hop communications.

For multihop wireless networks, we must simultaneously consider spectrum allocation and power control, which is a very important but difficult problem. Previous related work attempted to minimize power consumption [5], [6]. The optimal power-control scheme in [5] determines the power consumption per unit of data transmitted, and then, iteratively allocates the required data rate to different routes. In [6], a conflict-free spectrum allocation is deployed first, and joint route selection and power control is then designed using the spectrum allocation. To maximize throughput, the joint power and link-scheduling problem is formulated as a mixed integer linear programming problem in [7]. The objective function used is not the end-to-end (E2E) throughput but the sum of all the links’ throughput. In [8], Time Division Multiplexing (TDM) is used for link scheduling without considering transmit power.

Joint spectrum allocation and power control in multihop CRNs introduces several new challenges. First, the most important issue in CRNs is to protect primary users’ communications. Choosing an idle spectrum, allocating the spectrum to the links far away from the primary receivers using this spectrum, and applying power control to keep the interference to the primary users below the required limit must all be considered. Second, the spectrum condition changes according to the primary users’ activities, and hence, we need a strategy that adapts to the spectrum dynamics without incurring too much overhead in switching spectrum and route. An appropriate scheme of switching spectrum and route is, therefore, necessary to make a trade-off between the spectrum utilization and the switching overhead.

There have been only a few publications on routing and resource allocation for multihop CRNs. The authors of [9] described decoupled and collaborative interactions between route selection and spectrum management. In [10], a low-complexity algorithm is proposed to obtain a Pareto optimal solution for selecting a minimum-delay route. In [11], an on-demand routing protocol is proposed, also to minimize the delay, but with different delay definitions from those in...
In [10], a graph-coloring model is adopted for interference-free channel allocation. In the above-mentioned multihop CRNs, the secondary users are allowed to use the licensed spectrum only when it is not being used by the primary users, and power control was not considered at all. In practice, however, with proper power control, the secondary users can transmit data using low power that causes only acceptably low interference to the primary users’ communications. This way, the spectrum efficiency can be improved further.

In [14], joint channel and power allocation is investigated for CRNs. The authors of [15] focus on spectrum and power allocation in infrastructure-based CRNs. They consider the intercell interference for sharing the spectrum. In [16], interference temperature is adopted to restrict the interference to primary users. In [17], the spectrum sharing and routing problem is considered under the assumption that the set of available channels to each secondary user is static.

In [18] and [19], centralized and distributed schemes are proposed for CRNs, respectively. Both of them only consider different available channels at each node. In [20], the end-to-end throughput optimization problem is divided into two subproblems and is optimized using the Lagrangian duality. However, these approaches do not consider power control together with spectrum allocation for optimizing end-to-end throughput in a CRN. Moreover, they do not consider the dynamics of the available spectrum along with the resource allocation under an interference temperature model.

By contrast, in this paper, we address joint spectrum allocation and power control for secondary users which coexist with primary users on the same spectrum. We consider both the dynamic spectrum model [12] and the interference temperature model [16]. In the former, the primary users may not always use the spectrum, and hence, the secondary users can opportunistically utilize the spectrum when it is not being used by the primary users. In the latter, both primary and secondary users can coexist on the same spectrum. The secondary users’ interference to the primary receivers should not exceed the interference temperature limit. In most previous research, only one of these two models is considered for simplicity, but we consider both simultaneously; hence, addressing more general cases and improving the spectrum efficiency.

The main contributions of this paper are as follows:

- We present a new framework for characterizing the interplay among spectrum allocation and power control.
- We develop a TDM-based power-control scheme. An optimal time-partitioning strategy is derived to achieve the maximum end-to-end throughput, which is then used to evaluate the performance of each candidate route-spectrum combination.
- We develop a distributed spectrum allocation and power-control strategy for each flow. Nodes cooperate to deal with the interflow interferences and the cumulative interference temperature to enable the coexistence of multiple flows.
- The optimal waiting time before switching route and spectrum is derived by making a trade-off between the spectrum efficiency and the overhead of switching route and spectrum.

The rest of the paper is organized as follows: Section 2 describes the multihop network and spectrum models we will consider. Section 3 presents a new framework of joint spectrum allocation and power control in CRNs. Sections 4-6 describe power control, interflow coordination, and route-spectrum switch, respectively. Finally, the paper concludes with Section 7.

### 2 System Models

#### 2.1 Multihop Network Model

We consider a multihop CRN that consists of a set $\mathcal{N}$ of nodes and a set $\mathcal{L}$ of links. There is a set $\mathcal{K}$ of $K$ available spectrum bands. Each node is equipped with two radio interfaces, one for transmitting data and the other for receiving data, so the node can transmit and receive data at the same time. Like most typical wireless transceivers, the node can only work on one channel at a time for each interface. Table 1 lists the notations of the basic parameters in the network model.

Let $\gamma_l$ be the signal-to-interference ratio (SIR) on link $l$:

$$\gamma_l = \frac{p_l g_l}{\sigma^2 + \sum_{j \in \mathcal{L}(k(l)), j \neq l} P_j g_j},$$

where $k(l)$ is the spectrum on link $l$, $k(l) \in \mathcal{K}$, $\mathcal{L}(k)$ is the link set on spectrum $k$, and $\sigma^2$ includes not only the thermal noise, but also the interference from the primary users. According to Shannon’s capacity formula, the throughput over link $l$ can be modeled as a function of SIR:

$$R_l = W \log(1 + \gamma_l),$$

where $W$ is the bandwidth of a spectrum band.

Each node has a peak transmit power limit. The transmit power on each link should be kept below the peak power of its transmitter because of the equipment capability, i.e.,

$$p_l \leq p_{l_{\text{max}}},$$

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Meaning</th>
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<tbody>
<tr>
<td>$p_l$</td>
<td>transmit power of link $l$</td>
</tr>
<tr>
<td>$p_{l_{\text{max}}}$</td>
<td>peak transmit power of link $l$</td>
</tr>
<tr>
<td>$\gamma_l$</td>
<td>signal-to-interference ratio of link $l$</td>
</tr>
<tr>
<td>$g_l$</td>
<td>path gain from the transmitter of link $l$ to the receiver of link $l$</td>
</tr>
<tr>
<td>$h_{lm}$</td>
<td>path gain from the transmitter of link $l$ to primary receiver $m$</td>
</tr>
<tr>
<td>$Q_{mk_{\text{max}}}$</td>
<td>interference temperature limit at primary receiver $m$ on spectrum $k$</td>
</tr>
<tr>
<td>$Q_{mk}$</td>
<td>interference caused by flow $f$ at primary receiver $m$ on spectrum $k$</td>
</tr>
<tr>
<td>$R_l$</td>
<td>throughput of link $l$</td>
</tr>
<tr>
<td>$R_{f_{\text{end-to-end}}}$</td>
<td>end-to-end throughput of flow $f$</td>
</tr>
<tr>
<td>$R_{f_{\text{min}}}$</td>
<td>minimum throughput of the links which the data of flow $f$ go through on spectrum $k$</td>
</tr>
<tr>
<td>$U_{f_{\text{end-to-end}}}$</td>
<td>utility of flow $f$</td>
</tr>
<tr>
<td>$\theta_k$</td>
<td>effective time portion of spectrum $k$</td>
</tr>
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**Table 1**

List of the Basic Notations for the Network Model
The data of a set $F$ of flows from different source nodes are transmitted to their corresponding receivers/destinations in a multihop CRN. Suppose each flow is routed from its source to its destination via a single path. There is a set $M$ of $M$ primary receivers in the network. Primary users have priority over secondary users in accessing the spectrum; hence, restricting the secondary users’ spectrum usage as we describe next.

### 2.2 Spectrum-Activity Model

Two types of models have been proposed so far for the primary users’ spectrum usage activities: dynamic spectrum model [12] and interference temperature model [16].

According to the primary users’ spectrum usage pattern based on the experimental results in [21] and [22], the spectrum usage can be modeled as an ON-OFF process: ON (OFF) state represents when the spectrum is occupied (unoccupied) by primary users. In order to protect the primary users’ communications, the interference caused by secondary users must be kept below the interference temperature limit at the primary receivers. That is, the primary users’ Quality-of-Service (QoS) is acceptable if the secondary users’ interference is kept below a given interference temperature limit:

$$\sum_{l \in \mathcal{L}(k)} p_l b_{lm} \leq Q_{mk}^{\max}, \quad \forall m \in \mathcal{M}.$$  \hspace{1cm} (4)

Here, we assume that the interference temperature limits are known to the secondary users (cognitive radios) via some methods, such as use of dedicated control channels or backbone networks. In OFF state, the spectrum can be used by secondary users without considering their interference to primary users. It is assumed that the secondary users can obtain the perfect information on a primary user’s return.

The spectrum dynamics can be modeled as a semi-Markov process as in [23]. The lengths of ON and OFF periods are independent and identically distributed (i.i.d.). Table 2 lists the symbols used in the spectrum-activity model. These parameters of spectrum activities can be estimated by secondary users, e.g., using maximum likelihood (ML) estimators. The authors of [23] gave details of the ML method for estimating the distribution parameters, but it is beyond the scope of this paper.

### 2.3 Strategy-Switch Model

As mentioned earlier, the status of spectrum changes according to the primary users’ activities on the spectrum. To improve spectrum utilization, the SUs need to adapt their spectrum-use strategies. It takes the SUs a nonzero amount of time, say $t_S$, to switch their route and spectrum. During this time, no data transmission is allowed, thus incurring a switching overhead. Considering this overhead, it is not always efficient to make a switch immediately upon change of the spectrum status (ON $\rightarrow$ OFF or OFF $\rightarrow$ ON) because frequent route and spectrum switches will incur large overheads which may offset the gain achieved from the switchings. Therefore, for spectrum $k$, a route and spectrum switch is made only after waiting a certain amount of time, denoted by $T_{S,k}^{ON}$ and $T_{S,k}^{OFF}$ as defined in Table 2. Fig. 1 presents a state-transition diagram showing the transition conditions between the strategies associated with ON/OFF states.

During the waiting period (WP), a different strategy is used to protect primary users when the spectrum band makes an ON $\rightarrow$ OFF or OFF $\rightarrow$ ON transition as follows:

- **OFF $\rightarrow$ ON transition:** SUs do not transmit/receive any information to protect primary users, as WP1 and WP3 in Fig. 2.
- **ON $\rightarrow$ OFF transition:** SUs continue transmission/reception using the current strategy, as WP2 and WP4 in Fig. 2.

When there are $K(>2)$ spectrum bands, if the waiting time on one of the bands reaches the threshold of a corresponding switch, a route and spectrum switch will be made. Fig. 2 provides an example switch after WP3. When the waiting time on spectrum 3 reaches $T_{S,3}^{OFF}$, the strategy is switched.

![Fig. 1. Strategy-switch conditions with alternate spectrum ON/OFF status.](image-url)
3 Open Spectrum Utilization

Our problem is to enable the flows to utilize the spectrum efficiently, which can be stated formally as

\[
\max \sum_{f \in F} U_f(R_f)
\]

subject to the constraints of peak transmit power (3) and interference temperature limit (4). In this problem formulation, \(U_f(\cdot)\) is the utility function of data rate \(R_f\) for flow \(f\), which could be \(\log R_f\) for proportional fairness, or \(a_f R_f\) for maximum weighted throughput. \(R_f\) is the end-to-end throughput of flow \(f\) which is dictated by the link with the minimum throughput as

\[
R_f = \min_{l \in L(f)} R_l,
\]

where \(L(f)\) is the set of links through which flow \(f\) runs.

For efficient spectrum utilization, we propose a framework of joint spectrum allocation and power control for secondary users. In this framework, three subproblems are solved iteratively at different levels as follows:

3.1 Optimization for a Single Flow

This subproblem is to maximize \(R_f\) for each flow \(f\). Route and spectrum are jointly considered by selecting a strategy from all possible route-spectrum combinations based on the throughput to be achieved. We call a route-spectrum combination a spectrum-specified route (SSR). For each candidate SSR of a single flow, we estimate its end-to-end throughput. The throughput estimation is based on TDM-based power control, as we will describe in Section 4. We select the SSR with the maximum E2E throughput. Even though this subproblem is only for maximizing the E2E throughput of a single flow, it has to consider more complex factors, such as the interference/conflict between flows, allowable interference to primary users, and the inefficiency caused by spectrum dynamics. Therefore, we need to consider the following two subproblems together.

3.2 Optimization for Multiple Flows

The objective of this subproblem is to maximize \(\sum_{f \in F} U_f(R_f)\) during a period in which the states of channels do not change. According to our problem formulation, the binding constraints related to multiple flows are the interference in (1) and the interference temperature constraints (4). When the data of several flows are transmitted simultaneously in a multihop CR network, all flows will decide on their spectrum allocation and power control in a distributed manner. In order to achieve good performance and protect the primary users, these concurrent flows need to cooperate when selecting an SSR and determining the corresponding power level. This cooperation among multiple flows will be addressed in Section 5. The cooperation between flows will set some parameters for the flow-based distributed scheme, such as the successful transmission probability on a link with collisions considered, and a flow’s allowable interference to primary users.

3.3 Optimization in a Dynamic Spectrum Environment

This subproblem is to determine the optimal waiting time before making an SSR switch. If the PUs’ spectrum-usage pattern changes, the SSR should also be changed. If SSR switch immediately upon change of the spectrum status, each CR or SU may achieve better spectrum utilization, but frequent SSR switches will incur large overhead. Therefore, an SSR switch should wait for a certain amount of time, not immediately upon change of the spectrum status. In Section 6, we will make a trade-off between the spectrum efficiency and the spectrum switch overhead. Different values of the waiting time will yield different throughput loss of links, affecting the strategy decision when each flow optimizes its own objective.

4 TDM-Based Power Control for SSR

We first consider a simple case: the network with only a single flow. When selecting an SSR, we need to know the underlying power-control model in order to estimate the end-to-end throughput of each candidate SSR.

4.1 Power-Control Model

We propose a new parameter called the effective time portion and then divide the problem into several subproblems for each spectrum.

For a given SSR, instead of (6), the long-term mean end-to-end throughput of flow \(f\) is dictated by the bottleneck link on this path as

\[
R_f = \min_{l \in L(f)} \mathbb{E}[R_l],
\]

where \(\mathbb{E}[]\) is the expectation. In (7), the effective time portion \(\theta_k\) is introduced into the formulation of \(R_f\) for spectrum \(k\). If the strategy is determined with spectrum \(k\) in ON state, then \(\theta_k = 1\) because the SU does not change his strategy during the wait before making an SSR switch. If spectrum \(k\) is in OFF state, in order to protect PUs, the SU does not transmit/receive data during the wait after the spectrum changes to ON state, so a portion of time is used to avoid the interference to PUs, e.g., WP1 and WP3 in Fig. 2. The effective time portion for the spectrum in OFF state is

\[
\theta_k = \frac{\int_0^{\infty} t f_k^{OFF}(t) dt}{\int_0^{\infty} t f_k^{ON}(t) dt + \int_0^{\infty} t f_k^{OFF}(t) dt}.
\]
power over the links on the same spectrum. Let $R_k^f$ denote the minimum link throughput on spectrum $k$ on the path of flow $f$, then

$$R_k^f = \min_{i \in \mathcal{L}(f), k(i) = k} (\mathbb{E}[R_i]).$$

(9)

Based on the minimum throughput for each part of links, the E2E throughput of a flow, which is restricted by the minimum link throughput of the flow’s path, is dictated by the minimum of $R_k^f$ over the spectrum bands $k \in \mathcal{K}(f)$, where $\mathcal{K}(f)$ is the set of spectrum bands used by flow $f$:

$$R^f = \min_{k \in \mathcal{K}(f)} (\theta_k R_k^f).$$

(10)

This way, the throughput optimization problem of flow $f$ is decomposed into multiple subproblems $\max R_k^f$ for each spectrum $k$.

### 4.2 TDM-Based Suboptimal Power Control

Each link has its own transmitter and receiver, and transmissions over the links on the same spectrum may interfere with each other. This can be modeled as the interference channel model from an information-theoretic perspective [24], [25], which is still an open problem, even without interference temperature constraints. The optimal strategy for the capacity of interference channels depends on the interference coefficients, which correspond to the ratio of the path gains of interference signals to those of useful signals in the system model. From [24], TDM is known to be the best for moderate interference coefficients. For weak interference, TDM can achieve acceptable performance since the interference is low. In practice, a situation with strong interference can be made unlikely to occur with appropriate spectrum allocation. To make a trade-off between the performance and the complexity, we adopt TDM-based power control.

The vertices of the feasible power region are chosen as candidate power strategies. Let $N_k^f$ be the number of links that use spectrum $k$ on the path of flow $f$. $N_k^f$-dimensional feasible regions are bounded by both node peak transmit power and interference temperature constraints. In the information-theoretic TDM, only one link can transmit data in a time slot. By contrast, our proposed TDM can allow multiple links to transmit data simultaneously. We can thus achieve better performance than previously known analyses.

There are many vertices of the feasible power region, denoted as $p_{k,v}$ for link $l$ at vertex $v$, whose corresponding throughput is $R_{k,v}$. The expected throughput of link $l$ is

$$\mathbb{E}[R_l] = \sum_{v \in \mathcal{V}_k} \omega_{k,v} R_{k,v} P^{\text{succ}}_l(\omega_{k,v}),$$

(11)

where $\mathcal{V}_k$ is the set of all possible transmission combinations, $\omega_{k,v}$ is the time portion of the power strategy at vertex $v$ on spectrum $k$, and $P^{\text{succ}}_l(\omega_{k,v})$ is the successful transmission probability due to interflow transmission conflicts, which will be presented further in Section 5.1.

The problem is transformed from maximization of flow $f$’s end-to-end throughput to several subproblems of maximizing the minimum link throughput on each spectrum. The subproblem for spectrum $k$ can be stated as

$$\max \min_{i \in \mathcal{L}(f), k(i) = k} \left( \sum_{v \in \mathcal{V}_k} \omega_{k,v} R_{k,v} P^{\text{succ}}_l(\omega_{k,v}) \right),$$

(12)

subject to

$$\sum_{v \in \mathcal{V}_k} \omega_{k,v} = 1.$$  

(13)

To achieve the optimality, data should be transmitted over all links with the same throughput, i.e., all $\mathbb{E}[R_L]$’s are identical. Equation (11) can be transformed as

$$\sum_{v \in \mathcal{V}_k} \omega_{k,v} R_{k,v} P^{\text{succ}}_l(\omega_{k,v}) = \sum_{v \in \mathcal{V}_k} \omega_{k,v} R_{k,v} P^{\text{succ}}_l(\omega_{k,v}),$$

(14)

for all $i, j \in \mathcal{L}(f), k(i) = k, k(j) = k, i \neq j$.

So, we can solve (13) and (14) for $\omega_{k,v}$.

The number of candidate power vectors is always larger than that of links on the same spectrum, meaning that there are more undetermined parameters than the number of equations. Thus, the equations cannot be solved directly.

The optimal end-to-end throughput can be achieved in two cases. The first case is a linear combination of multiple power strategies. From a geometrical perspective, in the $N_k^f$-dimensional throughput space, the optimal end-to-end throughput is achieved at the maximum intersection point of the line that the throughputs of all links are the same, and the throughput polyhedron achieved by the power strategies at the vertices of the feasible power region. It must be the intersection point of the line and some $N_k^f$-dimensional hyperplane. This point can be constructed by a linear combination of at most $N_k^f$ vertices because it is on a hyperplane determined by $N_k^f$ vertices. In the second case, there exists a dominant power strategy that achieves larger throughputs of all links than those achieved by other strategies. The optimal solution adopts the dominant strategy.

The optimal power-control strategy, therefore, consists of at most $N_k^f$ strategies according to some time portion $\omega_{k,v}$. We can choose $N_k^f$ power vectors from the candidate power vectors and solve them using (13). After enumerating all the combinations for selecting power vectors, the maximum solution is chosen as the end-to-end throughput achieved on the SSR.

### 4.3 Reduction of Computational Complexity

The computational complexity of the power-control scheme increases exponentially with the number of links. Fortunately, the problem has already been decomposed into subproblems, one for each spectrum, so the number of links on a spectrum is usually not so large, lowering the complexity.

There are two other considerations in reducing the computational complexity. Omni-directional antennas are chosen for our study, and hence, it is inefficient if the node transmits and receives data on the same channel at the same time because of self-interference. Let $N^f$ be the number of links that flow $f$ runs through. The number of possible candidate SSRs for flow $f$ is $K(K - 1)^{(N^f - 1)}$, so the ratio of the reduced complexity is $(K - 1)K^{-(N^f - 1)}$ times more than the original one. If the geographic location information is available, then the node would not forward the data to any neighbor farther away from the destination [28]. To reduce the complexity, these inefficient cases are not
considered in the algorithm. Fig. 3 shows the ratio of the reduced complexity to the original complexity. According to the figure, these considerations can reduce complexity further when the number of channels gets smaller or the number of links becomes larger.

5 COOPERATION AMONG MULTIPLE FLOWS

For the multilink case, the interflow interference and the cumulative interference to PUs need to be considered for the selection of an SSR and a power-control strategy.

5.1 Cooperation on Interflow Interference

In order to control the interflow interference, we use the RTS/CTS scheme. When a node is receiving packets, its neighbors are not allowed to transmit. This causes the end-to-end throughput of the related flows to degrade, which needs to be considered in estimating the end-to-end throughput for SSRs.

To estimate the effect of collision among multiple flows, the nodes obtain the transmission probability information from their neighbors and calculate the probability of successful transmission. Since all flows are assumed to have same priority, each link has the same probability to successful transmission. Since all flows are assumed to need to be considered in estimating the end-to-end throughput for SSRs.

To calculate E2E throughput, we need to consider the successful probability. Considering the successful transmission probabilities, the power-control problem (12) in Section 4 can be solved by adjusting \( \omega_{k,v} \) and \( P_{l}^{\text{succ}}(\omega_{k,v}) \) iteratively.

This way, the nodes can estimate the effect of interflow interference by using only local information from their neighbors. If this cooperation is not deployed, the nodes may estimate the interflow interference only according to the a priori known node density.

5.2 Cooperation to Meet Cumulative Interference Temperature Constraints

A straightforward way of meeting the interference temperature constraints is to keep the allowable interference temperatures of each flow under \( 1/\left| F \right| \) of the total interference temperature constraints [29]. Recall that \( |F| \) is the number of flows. This conservative method can limit the interference, but will result in poor spectrum utilization, as a flow may be considered to cause the rise of interference temperature even when all the nodes on the flow’s path are far away from the PUs.

To get a distributed solution, we adopt decomposition based on the Lagrangian duality. Using the Lagrangian multiplier, we can rewrite the objective as

\[
\min_{\beta} D, \tag{17}
\]

where \( \beta \) is the vector of Lagrangian multipliers composed by \( \beta_{mk} \) for primary user \( m \) and spectrum \( k \). The dual function is

\[
D = \max_{f \in F} \sum_{m \in M} \sum_{v \in V} \beta_{mk} \left( \sum_{f \in F} Q_{mk}^f \right)
= \sum_{f \in F} \left( \max_{m \in M} \sum_{v \in V} \beta_{mk} Q_{mk}^f \right). \tag{18}
\]

In this method, the binding interference temperature constraint is decomposed for each flow. In order to share the allowable interference temperature among flows and improve spectrum utilization, each flow optimizes the following function:

\[
D_{f} = \max_{m \in M} U_{f} - \sum_{m \in M} \sum_{v \in V} \beta_{mk} Q_{mk}^f. \tag{19}
\]

By the Lagrangian multiplier method, the maximum \( \sum_{f \in F} U_{f} \) is proved to be achievable by maximizing \( D_{f} \) for each flow as in [30].

Note that the interference temperature information at the primary receivers is necessary for adjustment of \( \beta_{mk} \). In this way, the SU can determine \( \beta_{mk} \) according to the information collected locally from the primary receivers nearby to guarantee that

\[
\sum_{f \in F} Q_{mk}^f \leq Q_{mk}^{\text{max}}. \tag{20}
\]

If PUs cannot cooperate to report this required information to SUs, we need a controller that determines the values of \( \beta_{mk} \) to keep the interference temperature below the upper bounds \( Q_{mk}^{\text{max}} \). The controller collects the current interference.
temperature information from the primary receivers or sensors thereof. Using this information, it can adjust $\beta_{\text{net}}$ and announce the updated value to all of the flows. It is not necessary to have a whole-network-range controller that collects the related information from the whole network. Since a node causes little interference to the nodes far away from it, the controllers only need the local information inside the interference range, which pushes the proposed scheme to be more realistic.

5.3 Cooperation Gain

The noncooperative scheme is considered as the baseline for comparison. Corresponding to the interflow cooperation scheme, the noncooperative scheme is just the one without considering collision between multiple flows when calculating the E2E throughput for each SSR. For the cumulative interference temperature constraints, the noncooperative scheme keeps the interference temperature of each flow below $1/|\mathcal{F}|$ of the interference temperature constraints since there are $|\mathcal{F}|$ flows in the network. We evaluate the performance of four schemes: cooperation for both interflow interference and cumulative interference temperature constraints (IC-co), cooperation only for interflow interference (I-co), cooperation only for cumulative interference temperature constraints (C-co), and noncooperative schemes (non-co). The simulation configuration is set as in Section 7.2. We evaluate and compare the performances of the above four schemes.

Fig. 4a shows the improvement made by the proposed cooperation schemes. In this figure, with large interference temperature limits (i.e., more than -85 dBm in our case), the performance difference between IC-co and I-co is not noticeable; the same was also observed between C-co and non-co. This is because the cooperation on the cumulative interference temperature is unnecessary when the interference temperature is too large to restrict the transmit power.

Fig. 4b shows that the proposed scheme makes significant improvements in this case. When the number of nodes is small, some flows cannot find routes to their destinations. However, for those flows that can reach their destinations, their throughput is high as a result of small interferences. When the number of nodes gets larger (e.g., 30 nodes), almost all of flows can find routes to their destinations, but only a few candidate SSRs can be found and large interferences exist between flows because of large hop counts. Note that our proposed cooperation scheme cannot eliminate the interflow interference, but takes the interference into account for selection of the SSR and the transmit power. This is why the performance of the 20-node case is better than that of the 30-node case. When there are many nodes in the network, many routes can be found between them, and there is less interflow interference due to densely populated nodes. One can also see that for the 50-node case, the throughput of IC-co still increases as the number of nodes increases, while the other schemes are almost saturated.

In Fig. 4c, when there are only two flows, the improvement with cooperation for interflow interference is small. The difference between IC-co and C-co schemes gets larger as the number of flows increases, so does the performance difference between I-co and non-co. With a large number of flows, the cooperation for interflow interference can make significant effect. The cooperation for the cumulative interference temperature can also make a little performance improvement, but the difference for a different number of flows is not obvious from the simulation results.

All the simulation results show the improvement of the proposed cooperation schemes, which can achieve 10-40 percent more throughput than the noncooperation scheme.

6 OPTIMAL SSR SWITCH-WAIT TIME

When the state of some spectrum has changed for some predefined time, both route and spectrum need to be switched, triggering the SSR selection procedures again. The optimal switch-wait time should be calculated for each spectrum. For simplicity of expression, the spectrum index $k$ is omitted in this section. We now present a method for determining the optimal wait time $T_{\text{ON}}^S$ and $T_{\text{OFF}}^S$ by making a trade-off between spectrum efficiency and switch overhead.

6.1 Expected Throughput with Consideration of Switch Overhead

Our objective is to find the optimal switch-wait times $T_{\text{ON}}^S$ and $T_{\text{OFF}}^S$ to maximize the total throughput over a long time period. Since ON and OFF states alternate, we consider the expected throughput of one ON period and one OFF period. The objective becomes maximization of the expected throughput in a single ON-OFF period, instead of the average throughput over a long time period. The expected

[Fig. 4. Performance of the proposed algorithm with and without cooperation. (a) 30 nodes, 3 flows. (b) -100 dBm interference limit, 3 flows. (c) -100 dBm interference limit, 30 nodes.]
throughput during an ON period and an OFF period can be calculated as

\[ P_{00}R_{00} + P_{01}R_{01} + P_{11}R_{11} + P_{10}R_{10}, \]

(21)

where \( P_{00} \) and \( P_{01} \) are the probabilities that the strategy is designed for OFF and ON states, respectively, at the beginning of an OFF state, \( R_{00} \) and \( R_{01} \) are the expected throughput during an OFF period beginning with a strategy designed for OFF and ON period, respectively. \( P_{11} \), \( P_{10} \), \( R_{11} \), and \( R_{10} \) are defined similarly for the ON period.

The probabilities of initial strategies can be calculated by using state-transition probabilities. Fig. 5 shows the state-transition diagram. For the beginning of an OFF state, the probabilities of strategies can be calculated by using the probabilities of all possible transitions from the beginning of the last OFF state. For steady-state transition, the probabilities of beginning strategies in each OFF state should be same. For 00 state, there are two cases, 00 (last OFF state) → 10 (ON state) → 00 (OFF state) and 01 (last OFF state) → 10 (ON state) → 00 (OFF state). It can be obtained as

\[ P_{00} = P_{00}P(T_{ON} < T_{S_{ON}}) + P_{01}P(T_{OFF} < T_{S_{OFF}})P(T_{ON} < T_{S_{ON}}). \]

(22)

Similarly, the equation for 01 state can be obtained as

\[ P_{01} = P_{00}P(T_{ON} < T_{S_{ON}}) + P_{01}P(T_{OFF} < T_{S_{OFF}}) + P_{10}P(T_{OFF} > T_{S_{OFF}})P(T_{ON} > T_{S_{ON}}). \]

(23)

From (22) and (23), we get

\[ \frac{P_{00}}{P_{01}} = \frac{P(T_{OFF} > T_{S_{OFF}})P(T_{ON} > T_{S_{ON}})}{P(T_{ON} > T_{S_{ON}})}. \]

(24)

Since \( P_{00} + P_{01} = 1 \),

\[ P_{00} = \frac{P(T_{OFF} > T_{S_{OFF}})P(T_{ON} < T_{S_{ON}})}{P(T_{OFF} > T_{S_{OFF}})P(T_{ON} < T_{S_{ON}}) + P(T_{ON} > T_{S_{ON}})}. \]

(25)

\[ P_{01} = \frac{P(T_{ON} > T_{S_{ON}})}{P(T_{OFF} > T_{S_{OFF}})P(T_{ON} < T_{S_{OFF}}) + P(T_{ON} > T_{S_{ON}})}. \]

(26)

This way, the steady-state probabilities of the beginning strategies are obtained for OFF state. For ON state, \( P_{11} \) and \( P_{10} \) can also be obtained similarly as

\[ P_{11} = \frac{P(T_{ON} > T_{S_{ON}})P(T_{OFF} < T_{S_{OFF}})}{P(T_{ON} > T_{S_{ON}})P(T_{OFF} < T_{S_{OFF}}) + P(T_{OFF} > T_{S_{OFF}})}, \]

(27)

\[ P_{10} = \frac{P(T_{OFF} > T_{S_{OFF}})}{P(T_{ON} > T_{S_{ON}})P(T_{OFF} < T_{S_{OFF}}) + P(T_{OFF} > T_{S_{OFF}})}. \]

(28)

For calculation of the expected throughput with the beginning strategies, if the beginning strategy is consistent with the state, the SU will retain the beginning strategy. The strategies during the waiting time are different for ON and OFF states. The SUs do not transmit at all to protect PUs for the OFF → ON case, while the SUs continue to transmit using the beginning strategy for the ON → OFF case as shown in Fig. 6. \( R_H \) and \( R_L \) denote the achieved throughput of the strategies determined with the spectrum in OFF and ON periods, respectively. The expected throughput for each case can be calculated as

\[ R_{00} = R_H E(T_{OFF}) \]

(29)

\[ R_{01} = \int_0^{T_{S_{OFF}}} (R_L t)^{OFF}(t)dt + \int_{T_{OFF}+T_{S_{OFF}}}^{T_{OFF}+T_{S_{OFF}}} (R_L T_{S_{OFF}} + R_H (t - T_{OFF} - T_{S_{OFF}}))^{OFF}(t)dt, \]

(30)

\[ R_{11} = R_L E(T_{ON}) \]

(31)

\[ R_{10} = \int_{T_{S_{ON}}+T_{S_{OFF}}}^{T_{S_{ON}}+T_{S_{OFF}} (R_L (t - T_{ON} - t))^{ON}(t)dt. \]

(32)

We can find the optimal \( T_{S_{ON}} \) and \( T_{S_{OFF}} \) that maximize the throughput described as in (21). The ratio \( R_H/R_L \) can be predefined with a priori knowledge, or adjusted dynamically by learning from the recently achieved performance.
throughput is the achieved throughput at the beginning of OFF state, the achieved throughput is not change after waiting some time, and hence, the optimal solution is either adjust the strategy if the primary activity changes or not switch at all. We compare the above two solutions for an illustrative purpose.

In case of an exponentially distributed process due to its memoryless property, the expected remaining time would be larger for larger temperature limit, all the users transmit as the case that the interference temperature model, when a PU is transmitting, the nearby SUs are not allowed to transmit, which causes the loss of spectrum utilization. On the contrary, if the spectrum is utilized only according to the interference temperature model, when a PU is transmitting, the nearby SUs are allowed to transmit, which causes the loss of spectrum utilization. On the contrary, if the spectrum is utilized only according to the interference temperature model, then the spectrum activities are known, the optimal waiting time can be obtained by maximizing the objective function.

The performance with different switching overheads and switch gain ratios \( R_H / R_L \) is compared. From this figure, the expected throughputs decrease proportionally as the switching overhead increases. If the spectrum opportunities are utilized only according to the dynamic spectrum model, the performance is shown as the dash lines. Without considering the interference temperature model, when a PU is transmitting, the nearby SUs are not allowed to transmit, which causes the loss of spectrum utilization. On the contrary, if the spectrum is utilized only according to the interference temperature model, when a PU is transmitting, the nearby SUs are allowed to transmit, which causes the loss of spectrum utilization.

With a large enough switch overhead, the waiting time should be nonzero. Fig. 8 shows the minimum switching overhead if the switch-wait time is larger than 0.

The objective function for the Erlang-distributed process can be obtained by substituting the above equations into (21). Because the probability density functions of the spectrum activities are known, the optimal waiting time can be obtained by maximizing the objective function.

Fig. 7 shows the expected throughput for a three-order Erlang-distributed process in which \( \chi_{ON} = \chi_{OFF} = 30 \) s. The performance with different switching overheads and switch gain ratios \( R_H / R_L \) is compared. From this figure, the expected throughputs decrease proportionally as the switching overhead increases. If the spectrum opportunities are utilized only according to the dynamic spectrum model, the performance is shown as the dash lines. Without considering the interference temperature model, when a PU is transmitting, the nearby SUs are not allowed to transmit, which causes the loss of spectrum utilization. On the contrary, if the spectrum is utilized only according to the interference temperature model, when a PU is transmitting, the nearby SUs are allowed to transmit, which causes the loss of spectrum utilization.

With a large enough switch overhead, the waiting time should be nonzero. Fig. 8 shows the minimum switching overhead if the switch-waiting time is larger than 0. The minimum switching overhead for nonzero \( T_{OFF} \) is found to be larger for larger \( R_H / R_L \). In contrast, for nonzero \( T_{ON} \), the smaller \( R_H / R_L \), the larger minimum overhead, because the ratio of the change from 0 to \( R_L \) to the change from \( R_H \) to \( R_H \) with large \( R_H / R_L \) is relatively small compared to it in the case with small \( R_H / R_L \).

### 6.2 Optimal Waiting Time for Exponential and Erlang Distributions

To give an insight on the optimal switch-wait time, we consider the performance for exponential and Erlang-distributed ON/OFF processes. Note that the durations of ON and OFF periods do not have to follow these distributions; we only use these two distributions as examples for an illustrative purpose.

In case of an exponentially distributed process, the expected remaining time would not change after waiting some time, and hence, the optimal solution is either adjust the strategy if the primary activity changes or not switch at all. We compare the above two solutions for an illustrative purpose.

In case of an exponentially distributed process due to its memoryless property, the expected remaining time would not change after waiting some time, and hence, the optimal solution is either adjust the strategy if the primary activity changes or not switch at all. We compare the above two solutions for an illustrative purpose.

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The definition of the standard function has three conditions.

1. **Positivity:** \( I(\omega) > 0 \).
2. **Monotonicity:** If \( \omega \geq \omega' \), then \( I(\omega) \geq I(\omega') \).
3. **Scalability:** For all \( \alpha > 1 \), \( \alpha I(\omega) > I(\alpha \omega) \).

The positivity and the monotonicity of the update function are satisfied according to the expression of the success probabilities, respectively. Therefore, 

\[
\omega \geq I(\omega). \quad (38)
\]

In order to guarantee the efficient transmission time \( T \), the update function of \( \omega \) in the proposed iterative algorithm is presented as

\[
I_{\text{su}}(\omega) = \frac{T}{I_{\text{su}}(\omega)}. \quad (39)
\]

In [31], the iterative algorithm can converge to a unique fixed point if the update function is a standard function. The definition of the standard function has three conditions for all \( \omega > 0 \):

- **Positivity:** \( I(\omega) > 0 \).
- **Monotonicity:** If \( \omega \geq \omega' \), then \( I(\omega) \geq I(\omega') \).
- **Scalability:** For all \( \alpha > 1 \), \( \alpha I(\omega) > I(\alpha \omega) \).

The performance of the proposed algorithms is evaluated using dynamic system-level simulation with OPNET. Primary and secondary users/devices/nodes are uniformly placed in a 100 m \( \times \) 100 m area. The path gain between nodes is modeled as

\[
P_L = \frac{P_{L_0} \cdot D / D_0}{\lambda} \quad \text{where} \quad D = \text{distance.}
\]

The simulation results are shown using error bars. For performance comparison, we consider two existing schemes, RDSA [8] and TRSS [20]. RDSA maximizes the E2E throughput by link scheduling with cochannel interference, and TRSS considers link scheduling for spectrum sharing together with a binary interference model. The simulation results in Fig. 9 demonstrate the performance improvement of the proposed algorithm which considers power control together with other aspects of resource allocation.

Compared with TRSS, in Fig. 9a, the performance improvement is not obvious when the interference temperature limit is large, because the power control is not so important if the transmit power is not restricted. Fig. 9b shows the proposed scheme to achieve better performance when the number of secondary nodes is small or large.
enough. When the number of secondary nodes is moderate (e.g., 30 nodes), the performances of TRSS and the proposed algorithm are similar because of serious interflow conflicts, as same as it shown in Fig. 4. Fig. 9c shows the performance improvement to increase as the number of flows increases. The confidence interval of the proposed algorithm is larger than TRSS because the effect of power control in the proposed algorithm makes a significant performance gain in certain (not all) topologies, causing the large confidence interval.

From the simulation results, one can see that the performance of RDSA is much worse than that of the proposed scheme in CRNs with interference temperature limits. The maximum power is used, causing too large interference to primary users. Therefore, a number of links near PUs are unavailable. Especially, in Fig. 9a, when the interference temperature limit is tight (e.g., -115 dBm), almost all the links are disconnected and only a few flows can be transmitted from sources to destinations successfully, so the average total throughput is low. In such a case, for RDSA algorithm, the ratio of the confidence interval to the average value is large.

The confidence interval decreases with the increasing number of random topologies. Here, we pay more attention to the relative values of the proposed algorithm in various scenarios with different parameters. In most cases, as shown in Figs. 9b and 9c, the confidence interval is larger if the corresponding average value is larger. By contrast, in Fig. 9a, when the interference temperature limit increases, the total throughput increases with the decreasing confidence interval. When the interference temperature limit is small, the random positions of primary users affect the stability of throughput performance.

8 CONCLUSIONS AND FUTURE WORK

In this paper, joint spectrum allocation and power control is proposed to utilize open spectrum bands in CRNs by considering both interference temperature constraints and spectrum dynamics. A TDM-based power-control strategy is adopted to achieve maximum end-to-end throughput, which is used to evaluate the performance of each candidate SSR in choosing an appropriate multihop route and its corresponding spectrum for a single flow. In multihop networks, each flow determines its own strategy in a distributed manner. Both interflow and cumulative interference temperatures are considered in the cooperative schemes. Considering the overhead of switching routes and spectra, the optimal wait time is derived using a probabilistic approach. A balance is achieved by making a trade-off between spectrum efficiency and the overhead of switching routes and spectrum bands. Our simulation results show that the proposed cooperative schemes utilize the spectrum very efficiently.

In this paper, the spectrum bands are assumed independent of each other. The interaction between spectrum bands will be considered in our future work. The authors of [33] showed that the spectrum activities are correlated in the frequency domain. The phenomenon of power leakage also increases the interference between adjacent channels.

APPENDIX A

PROOF OF SUCCESSFUL TRANSMISSION PROBABILITY

Following the discussion in Section 5.1, in order to accurately evaluate the end-to-end throughput of candidate SSRs, the successful transmission probability is proposed to account for the conflict between multiple flows. The expression of the successful transmission probability can be proved to be correct by mathematical induction.

The successful transmission probability (16) can be rewritten as

$$P_{\text{succ}}(\omega, \omega_1, \ldots, \omega_N) = 1 - \phi_1 \sum_{1 \leq i \leq N} \omega_i + \phi_2 \sum_{1 \leq i, j \leq N, i \neq j} \omega_i \omega_j + \cdots + \phi_N \omega_1 \ldots \omega_N,$$

where the coefficients are

$$\phi_n = (-1)^n \frac{1}{n+1}.$$

For easier understanding, we take link A with two neighbor links as an example. The probability that link A wants to transmit is \(\omega\), but the actual successful transmission probability is lower than \(\omega\) due to collisions. The probability that link A’s transmission conflicts with one of two neighbor links is \(\omega \omega_1\) and \(\omega \omega_2\), respectively. In these two cases, link A can occupy the spectrum with only 50 percent of the time. To compute the successful transmission probability, \(1/2(\omega \omega_1 + \omega \omega_2)\) is subtracted from the transmission probability. However, there is a case when all three links want to transmit at the same time. The probability of such an event is \(\omega \omega_1 \omega_2\), and \((1 - 1/3)\omega \omega_1 \omega_2\) should be subtracted from the transmission probability. This part must be subtracted \(C_3^1\) times for collision between link A and one of its two neighbor links.

This way, the coefficient for the collision of link A and n neighbor links can be calculated as

$$\phi(n) = -\left(1 - \frac{1}{n+1}\right) - \sum_{k=1}^{n-1} C_n^k \phi_k,$$

where

$$C_n^k = \frac{n!}{(n-k)!k!}.$$

The next step is to derive the coefficients of the expression (see (43)). The first coefficient \(\phi_1\) can be calculated by using (44):

$$\phi_1 = -\left(1 - \frac{1}{1+1}\right) = -\frac{1}{2} = (-1)^1 \frac{1}{1+1}. \quad (45)$$

Similarly, when \(n = 2\), \(\phi_2\) can be written as

$$\phi_2 = -\left(1 - \frac{1}{2+1}\right) - C_2^1 \left(-\frac{1}{2}\right) = \frac{1}{3} = (-1)^2 \frac{1}{2+1}. \quad (46)$$

For these basic cases, the coefficient expression (43) holds.

Suppose (43) holds for all the elements from \(\phi_1\) to \(\phi_n\). For \(\phi_{n+1}\),
\[
\phi_{n+1} = -\left(1 - \frac{1}{n+2}\right) - \frac{n}{n+2} \sum_{k=1}^{n} C_{n+1}^{k} \phi_{k}
\]

(47)

Because of

\[
\frac{1}{k+1} C_{n+1}^{k} = \frac{1}{n+2} C_{n+2}^{k+1},
\]

\[
\phi_{n+1} \text{ can be expressed as}
\]

\[
\phi_{n+1} = -\frac{n+1}{n+2} + \frac{1}{n+2} \sum_{k=1}^{n+1} C_{n+2}^{k}(-1)^{k}.
\]

Substituting \( k \) for \( k + 1 \),

\[
\phi_{n+1} = -\frac{n+1}{n+2} + \frac{1}{n+2} \sum_{k=2}^{n+2} C_{n+2}^{k}(-1)^{k} \frac{1}{n+2}
\]

\[
-1 + (n + 2) - (-1)^{n+2}
\]

\[
= (-1)^{n+2} \frac{1}{n+2}
\]

\[
= (-1)^{n+1} \frac{1}{n+1} + 1.
\]

The above condition can be transformed to

\[
(\alpha - 1) - \frac{1}{2}(\alpha^{2} - 1)\psi_{1} + \frac{1}{3}(\alpha^{3} - 1)\psi_{2} + \cdots
\]

\[
+ (-1)^{N} \frac{1}{N+1}(\alpha^{N+1} - 1)\psi_{N} > 0.
\]

(54)

Because of \( \alpha - 1 > 0 \),

\[
1 - \frac{1}{2}(\alpha + 1)\psi_{1} + \frac{1}{3}(\alpha^{2} + \alpha + 1)\psi_{2} + \cdots
\]

\[
+ (-1)^{N} \frac{1}{N+1}(\alpha^{N} + \alpha^{N-1} + \cdots + 1)\psi_{N} > 0.
\]

(55)

According to the relationship of sets, it can be obtained that

\[
\psi_{k} > \alpha \psi_{k+1}.
\]

(56)

Based on (56), two neighbor terms can be canceled by each other.

\[
\frac{1}{k+1} (\alpha^{k} + \alpha^{k-1} + \cdots + 1)\psi_{k}
\]

\[
- \frac{1}{k+2} (\alpha^{k+1} + \alpha^{k} + \cdots + 1)\psi_{k+1}
\]

\[
> \left( \frac{1}{(k+1)(k+2)} (\alpha^{k+1} + \alpha^{k} + \cdots + 1) - \frac{1}{k+2} \right)\psi_{k+1}
\]

\[
> 0.
\]

(57)

When \( N \) is an odd number, (55) is satisfied as

\[
1 - \frac{1}{2}(\alpha + 1)\psi_{1} + \frac{1}{3}(\alpha^{2} + \alpha + 1)\psi_{2} + \cdots
\]

\[
+ (-1)^{N} \frac{1}{N+1}(\alpha^{N} + \alpha^{N-1} + \cdots + 1)\psi_{N}
\]

\[
= \left( 1 - \frac{1}{2}(\alpha + 1)\psi_{1} \right) + \cdots
\]

\[
+ \left( (-1)^{N-1} \frac{1}{N}(\alpha^{N-1} + \cdots + 1)\psi_{N-1} \right)
\]

\[
+ (-1)^{N} \frac{1}{N+1}(\alpha^{N} + \alpha^{N-1} + \cdots + 1)\psi_{N}
\]

\[
> 0.
\]

(58)

When \( N \) is an even number, (55) is also satisfied as

\[
1 - \frac{1}{2}(\alpha + 1)\psi_{1} + \frac{1}{3}(\alpha^{2} + \alpha + 1)\psi_{2} + \cdots
\]

\[
+ (-1)^{N} \frac{1}{N+1}(\alpha^{N} + \alpha^{N-1} + \cdots + 1)\psi_{N}
\]

\[
= \left( 1 - \frac{1}{2}(\alpha + 1)\psi_{1} \right) + \cdots
\]

\[
+ \left( (-1)^{N-2} \frac{1}{N-1}(\alpha^{N-2} + \cdots + 1)\psi_{N-2} \right)
\]

\[
+ \left( (-1)^{N-1} \frac{1}{N}(\alpha^{N-1} + \cdots + 1)\psi_{N-1} \right)
\]

\[
+ (-1)^{N} \frac{1}{N+1}(\alpha^{N} + \alpha^{N-1} + \cdots + 1)\psi_{N}
\]

\[
> \frac{1}{N+1}(\alpha^{N} + \alpha^{N-1} + \cdots + 1)\psi_{N} > 0.
\]
Therefore, the update function of the proposed iterative algorithm satisfies the scalability condition of the standard function.

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