

Supplement of “Modeling and Real-time Scheduling of Large-Scale Batteries for Maximizing Performance”

Eugene Kim and Kang G. Shin

Department of Electrical Engineering and Computer Science
The University of Michigan – Ann Arbor, U.S.A.
{kimsun,kgshin}@umich.edu

Jinkyu Lee

Department of Computer Science and Engineering
Sungkyunkwan University (SKKU), Republic of Korea
jinkyu.lee@skku.edu

I. ALGORITHM FOR IN A CYCLE

To minimize energy consumption of auxiliary devices, we must consider both energy consumption of batteries and UCs. Therefore, we compare the power consumption at each control interval so as to search the set of discharge current of battery for the minimum energy consumption by using the battery voltage model as shown in Algorithm 1. In a

Algorithm 1 Algorithm for the target current calculation

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1: procedure ICAL( $n, P_{\text{req}}, I_{\text{bat}}^*, T_{\text{bat}}$ )
2:   for  $i == 0; i < n; i++$  do
3:      $I_{\text{tot}} = \frac{P_{\text{req}}}{V_o}$ ;
4:      $I_{\text{UC}}[i] = 0$ ;
5:      $I_{\text{bat}}[i] = I_{\text{tot}}$ ;
6:     while  $I_{\text{bat}}[i] > I_{\text{bat}}^* \ \& \ E(I_{\text{bat}}[i], I_{\text{UC}}[i], T_{\text{bat}}[i]) > E(I_{\text{bat}}[i] -$ 
7:        $1, I_{\text{UC}}[i] + 1, T_{\text{bat}}[i])$  do
8:          $j \leftarrow \text{FindPrechargePeriod}();$  //
9:         if  $j == \text{NULL}$  then
10:           Break;
11:         else
12:            $I_{\text{UC}}[i] \leftarrow I_{\text{UC}}[i] + 1$ ;
13:            $I_{\text{bat}}[i] \leftarrow I_{\text{bat}}[i] - 1$ ;
14:            $I_{\text{UC}}[j] \leftarrow I_{\text{UC}}[j] - 1$ ; // Precharge UC at time  $j$ 
15:            $I_{\text{bat}}[j] \leftarrow I_{\text{bat}}[j] + 1$ ; // Precharge at time  $j$ 
16:         end if
17:       end while
18:     end for
19:   return  $[I_{\text{bat}}, I_{\text{UC}}]$ ;
20: end procedure

```

vehicle system, energy consumption occurs in a battery and auxiliary devices. This energy consumption can be estimated by integrating power consumptions ($E_{\text{total}} = \int_0^T P_{\text{total}}(t)dt$), and Sec. III shows how to calculate the power requirements. To maximize battery operation-time (t_{op}), we have to remove as many voltage drop periods as possible. So, we iteratively find the voltage drop period and compensate the voltage by regulating battery temperature as seen in Algorithm 2.

Algorithm 2 provides offline temperature scheduling for a given power requirement, and an insight on how to schedule temperature in real-time. According to the scheduling results, battery temperature should be increased when it cannot supply the required power, which is estimated by using the battery output voltage model. We determine the target temperature based on the output voltage model. It makes battery operate first at a low temperature because initially battery SoC is enough to supply the required power to the electric load. Then, we increase battery temperature as the SoC goes down while regulating battery temperature based on the power requirement prediction. That is, when a large power requirement is predicted, we increase temperature to decrease battery internal

Algorithm 2 Algorithm for the target temperature

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1: procedure TCAL( $n, T_{\text{bat}}^*, I_{\text{bat}}$ )
2:   for  $i == 0; i < n; i++$  do
3:      $T_{\text{bat}}[i] = T_{\text{bat}}^*$ ;
4:   end for
5:   for  $i == 0; i < n; i++$  do
6:     while  $V_{\text{bat}}(I_{\text{bat}}[i], T_{\text{bat}}[i]) < V_{\text{lb}}$  do
7:        $j \leftarrow \text{FindCoolingPeriod}();$ 
8:       if  $j == \text{NULL}$  then
9:         Break;
10:      else
11:         $T_{\text{bat}}[i] \leftarrow T_{\text{bat}}[i] + 1$ ;
12:         $T_{\text{bat}}[j] \leftarrow T_{\text{bat}}[j] - 1$ ; // Cooling at time  $j$ 
13:      end if
14:    end while
15:  end for
16:  return  $[T_{\text{bat}}]$ ;
17: end procedure

```

resistance. After determining the target discharge current, we calculate the temperature scheduling period by considering its reliability in the worst case such that maximum current is discharged from battery. That is, we have to consider the possibility of reaching an upper bound of temperature when maximum available current is discharged based on thermal transfer function. Note that temperature scheduling period would be longer than current scheduling period, since battery temperature changes more slowly than battery current.

Algorithm 3 Algorithm for real-time temperature scheduling

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1: procedure PROC4( $I_{\text{bat}}^*, T_{\text{bat}}^*$ )
2:   while Driving do
3:     while  $V_o^* + V_{\text{margin}} < V_o(I_{\text{bat}}^*, T_{\text{bat}}^*)$  do
4:        $T_{\text{bat}}^* --$ ;
5:     end while
6:     while  $V_o^* + V_{\text{margin}} > V_o(I_{\text{bat}}^*, T_{\text{bat}}^*)$  do
7:        $T_{\text{bat}}^* ++$ ;
8:     end while
9:     Sleep( $p_T$ );
10:  end while
11: end procedure

```

II. BATTERY DEGRADATION

Fig. 1 shows battery degradation at some temperature. First, initial degradation level was $8.32 \text{ m}\Omega$. After 37 discharge/charge cycles, it became $9.02 \text{ m}\Omega$. That is, average degradation was $18.9 \mu\Omega$ for a cycle. Therefore, we assumed its change has a negligible influence on battery capacity within a cycle in the paper.

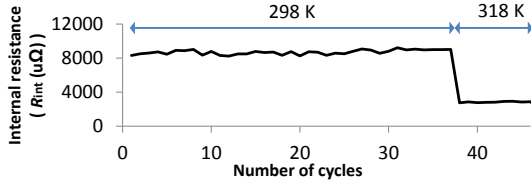


Fig. 1. An example of battery degradation: During the first 37 cycles, the battery operates at 298K, 1 A of the average discharged current ($\frac{1}{t_o^k} \int_0^{t_o^k} I_{bat}(t) dt$ ($\frac{1}{t_o^k} Q_d^k$)), and 1.5A of the average amount of battery discharge/charge current ($\frac{1}{t_o^k} \int_0^{t_o^k} |I_{bat}(t)| dt$), and the battery operates at 318K with the same condition after 38 cycle.

III. POWER REQUIREMENT FOR BMS IN EVS

To supply required power (P_{req}) for operating electric motors of vehicles, energy should be extracted from energy storages and auxiliary devices while inducing power loss (P_{total}) as follows:

$$P_{total}(t) = P_{battery}(t) + P_{UC}(t) + P_{converter}(t) + P_{cooler}(t).$$

Supplying power from batteries to electric load induces voltage drop with power loss on battery $P_{battery}(t)$ due to battery's non-idealistic properties.

$$P_{bat}(t) = (V_{oc}(t) - V_o(t)) \cdot I_{bat}(t),$$

where $V_{oc}(t)$ is open circuit voltage, $V_o(t)$ is output voltage, and $I_{bat}(t)$ is discharged current. Also, auxiliary devices for mitigating discharging stress dissipate energy in path from UC ($P_{UC}(t)$) and converter ($P_{conv}(t)$) to electric load.

$$P_{UC}(t) = I_{UC}(t)^2 \cdot R_{UC},$$

$$P_{converter}(t) = I_{UC}(t)^2 \cdot R_{converter}.$$

In addition, cooler for regulating batteries' temperature causes power dissipation ($P_{cooler}(t)$).

$$P_{cooler}(t) = f_{cooler}(\Delta T(t)),$$

where $\Delta T(t)$ is target battery temperature changes for thermal management.

IV. POWER REQUIREMENT FOR EVALUATIONS

We extracted realistic power requirements for real driving data from "The US Environmental Protection Agency (EPA)" and "California Air Resources Board" by using the vehicle simulator as shown in Fig. 2.

V. EXTRACTED GENES

We extracted the most effective genes for building battery models via the algorithm in the paper. Fig. 3 and 4 represents the extracted genes for predicting battery output voltage (V_o) and battery degradation rate (ΔR_{int}) in the order of occurrence, respectively. In Fig. 3, x1 is battery temperature ($T_{bat}(t)$), x2 the rate change of battery current ($\frac{dI_{bat}}{dt}(t)$), x3 is a battery discharge/charge current ($I_{bat}(t)$), x4 the amount of discharged charge ($Q_d(t)$), and x5 the rate change of battery voltage ($\frac{dV_{bat}}{dt}(t)$), respectively. In Fig. 4, x1 is a previous degradation rate (R_{int}), x2 accumulative temperature exposure ($\int_0^{t_o^k} T_{bat}(t) dt$), x3 the amount of discharged charge

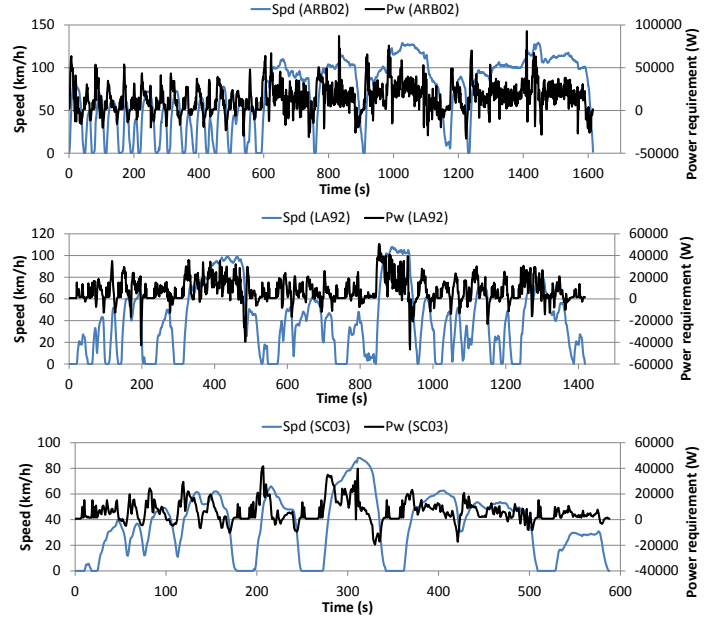


Fig. 2. Power requirements for driving patterns (ARB02, LA92, SC03)

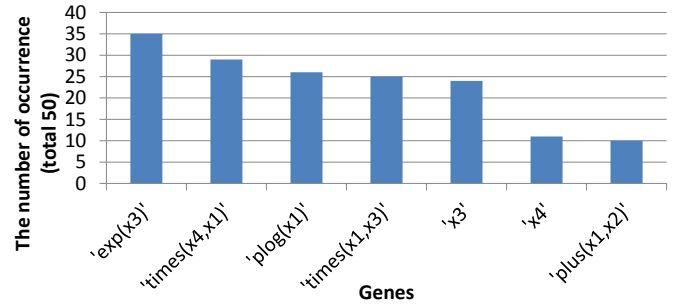


Fig. 3. The most commonly extracted genes for battery voltage model.

(Q_d^k), and x4 the average amount of discharge/charge current ($\frac{1}{t_o^k} \int_0^{t_o^k} |I_{bat}(t)| dt$), respectively.

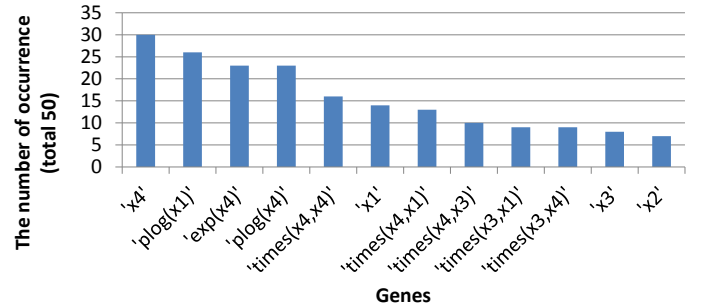


Fig. 4. The most commonly extracted genes for battery degradation model.